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# Experimental

# Information on V<sub>us</sub>

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#### UNITARY SYMMETRY AND LEPTONIC DECAYS

Nicola Cabibbo CERN, Geneva, Switzerland (Received 29 April 1963)

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#### First Row CKM Unitarity Relation

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \sim \begin{pmatrix} 1 & \lambda & \lambda^3 \\ \lambda & 1 & \lambda^2 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix}$$
$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1 - \Delta \qquad \begin{array}{c} \Delta & \text{was} \sim 2\sigma \\ \text{up to } 2004 \\ \text{up to } 2004 \\ \text{up to } 2004 \end{array}$$

### First Row CKM Unitarity Relation

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \sim \begin{pmatrix} 1 & \lambda^3 \\ \lambda & \lambda^3 \\ \lambda^3 & \lambda^2 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix}$$
$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1 - \Delta \qquad \Delta \operatorname{was} \sim 2\sigma \\ \operatorname{negligible}_{|V_{ub}| = (3.93 \pm 0.36) \cdot 10^{-3}}$$

- Super-allowed  $0^+ \rightarrow 0^+$  Nucleus-Decays
- Neutron β-Decay measurement Neutron lifetime measurements
- Pion  $\beta$ -Decay measurement

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|\mathbf{V}_{ud}| = 0.97425 \pm 0.00022
Phys.Rev.C79 (2009) 055502
Towner - Hardy
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### First Row CKM Unitarity Relation

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \sim \begin{pmatrix} 1 & \lambda & \lambda^{3} \\ \lambda & \lambda & \lambda^{2} \\ \lambda^{3} & \lambda^{2} & 1 \end{pmatrix}$$
$$|V_{ud}|^{2} + |V_{us}|^{2} + |V_{ub}|^{2} = 1 - \Delta \qquad \Delta \text{ was } \sim 2\sigma \text{ up to } 2004 \text{ negligible} \\ |\nabla_{ub}| = (3.93 \pm 0.36) \cdot 10^{-3} \qquad V_{us} \cdot \cdot \cdot$$
$$\cdot \text{ Super-allowed } 0^{+} \rightarrow 0^{+} \text{ Nucleus-Decays} \qquad \cdot \text{ Semileptonic kaon decays} \\ \cdot \text{ Neutron } \beta\text{-Decay measurement} \qquad \cdot \text{ Leptonic kaon decays}$$

- Tau decays into kaon final states
  - Improved theory (lattice,  $\chi PT$ , OPE, ...)

 $\Delta = 0 \Rightarrow |V_{us}| = 0.2255 \pm 0.0010$ Most precise test of CKM Unitarity

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Towner - Hardy

Neutron lifetime measurements

 $|V_{ud}| = 0.97425 \pm 0.00022$ 

Phys.Rev.C79 (2009) 055502

• Pion β-Decay measurement

#### Outline



#### **Kaon Decays**

- Semileptonic K<sub>13</sub>
- Leptonic  $K_{12}/\pi_{12}$



- → see M. Antonelli talk!
- → see Ch. Sachrajda, J. Bijnens, U. Heller, I. Rosell, H. Neufeld talks!

#### **Tau Decays**

- Inclusive using OPE
- Exclusive  $\tau \rightarrow K\nu/\pi\nu$





# V<sub>us</sub> from Kaon Decays



$$\Gamma_{Kl3} = \frac{G_F^2 \cdot M_K^5}{192 \pi^3} S_{EW} | V_{us} | f_+^2(0) \cdot I^{Kl}(\lambda_I) \cdot (1 + \delta_{EM})$$

Partial Decay Width (Experiment) → BR's → Lifetimes

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Experimental Information on  $V_{us}$ 

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*Theoretical challenge:*  $f_+(0)$ 





- Discrepancy btw. Lattice and ChPT, which tends to give higher values for  $f_+(0)$
- Trend is to use lattice results,

FLAVIANET FLAG recommendation:  $f_+(0) = 0.9644(49)$  RBC/UKQCD '07

Summary  $V_{us}$  from  $K_{l3}$  Decays



#### $K_{l3}$ average: $|V_{us}| f_{+}(0) = 0.21660(47)$

With  $f_{+}(0) = 0.9644(49)$  from lattice QCD:

$$K_{l3}$$
 average:  $|V_{us}| = 0.2246(12)$ 

Using  $|V_{ud}| = 0.97425(22)$  (Towner-Hardy '09)

$$V_{ud}^2 + V_{us}^2 - 1 = -0.0004(7)$$
  
Compatibility with unitarity  $-0.6\sigma$ 

was 0.031(15) in PDG04

 $V_{\mu s}$  from  $K_{12}$  Decays



 $\frac{[1.189(7)]^2 \text{HPQCD/UKQCD 08}}{\Gamma(K_{\mu 2(\gamma)})} = \frac{|V_{us}|^2}{|V_{ud}|^2} \frac{f_K^2}{f_\pi^2} \frac{m_K (1 - m_\mu^2 / m_K^2)^2}{m_\pi (1 - m_\mu^2 / m_\pi^2)^2} \begin{bmatrix} 1 + \alpha (C_K - C_\pi) \end{bmatrix}$ 

**Inputs from experiment:** 

KLOE: BR $(K^{\pm}_{\mu 2(\gamma)}) = 0.6347(18)$  $\tau_{K\pm} = 12.384(15) \text{ ns}$ 

PDG: BR $(\pi^{\pm}_{\mu^{2}(\gamma)}) = 0.9999$  $\tau_{\pi^{\pm}} = 26.033(5)$  ns

 $|V_{us}|/|V_{ud}| = 0.2319(15)$  $|V_{us}| = 0.2259(15)$ 

 $V_{\mu s}$  from  $K_{12}$  Decays



 $\frac{[1.189(7)]^2 \text{HPQCD/UKQCD 08}}{\Gamma(K_{\mu 2(\gamma)})} = \frac{|V_{us}|^2}{|V_{ud}|^2} \frac{f_K^2}{f_\pi^2} \frac{m_K (1 - m_\mu^2 / m_K^2)^2}{m_\pi (1 - m_\mu^2 / m_\pi^2)^2} \begin{bmatrix} 0.9930(35) \text{ Marciano '04} \\ 1 + \alpha (C_K - C_\pi) \end{bmatrix}$ 0.23 68% C.L.s **Inputs from experiment:**  $V_{ud}$ Vus KLOE:  $V_{us} V_{ud}$  $BR(K^{\pm}_{\mu 2(\gamma)}) = 0.6347(18)$  $\tau_{K\pm} = 12.384(15)$  ns 0.225  $V_{us}$ **PDG:** BR( $\pi^{\pm}_{\mu 2(\gamma)}$ ) = 0.9999 unitarity  $\tau_{\pi\pm} = 26.033(5)$  ns  $|V_{us}|/|V_{ud}| = 0.2319(15)$  $V_{ud}$ 0.22 – 0.97  $|V_{us}| = 0.2259(15)$ 0.975

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# V<sub>us</sub> from Tau Decays



The branching fractions and invariant mass distributions are the experimental input to determine  $V_{us}$  from  $\tau$ .

## $V_{us}$ : The Master - Formula for $\tau$ - Decays



The branching fractions and invariant mass distributions are the experimental input to determine  $V_{us}$  from  $\tau$ .

### $V_{us}$ : The Master - Formula for $\tau$ - Decays



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### *B* - *Factories are also* $\tau$ - *Factories*

At  $\Upsilon(4S)$  energies:  $\sigma(e^+e^- \rightarrow \tau^+\tau^-) \sim \sigma(e^+e^- \rightarrow BB) \sim 0.9$  nb  $\rightarrow$  Huge tau rates  $\rightarrow$  Tagging



- Both experiments have a very large ( $\sim 10^9$ ) sample of tau events
- Detectors are well matched to do tau physics:
  - K/ $\pi$  particle ID,  $\gamma/\pi^0$  reconstruction, charged particle tracking, etc.
- Can reduce most non-tau backgrounds to  $\leq 1\%$ :
  - Bhabhas,  $\mu$ -pairs,  $e^+e^- \rightarrow q\bar{q}$

## Recent $\tau$ Results relevant for $V_{us}$

Mode	BaBar		Belle Selle	
τ-→π <sup>-</sup> ν	Preliminary ICHEP08	467 fb <sup>-1</sup>		
<b>τ</b> -→K <sup>-</sup> ν	Preliminary ICHEP08	467 fb <sup>-1</sup>		
$\tau \rightarrow K^0 \pi^- \nu$	Preliminary ICHEP08	385 fb <sup>-1</sup>	PLB654(2007) 65	351 fb <sup>-1</sup>
$\tau \rightarrow K^{-}\pi^{0}\nu$	PRD76(2007)051104	230 fb <sup>-1</sup>		
$\tau \rightarrow \pi^{-}\pi^{-}\pi^{+}\nu$	PRL100(2008)011801	342 fb <sup>-1</sup>		
$\tau \rightarrow K^{-}\pi^{-}\pi^{+}\nu$	PRL100(2008)011801	342 fb <sup>-1</sup>	Preliminary ICHEP08	500 fb <sup>-1</sup>
$\tau \rightarrow K^{-}\pi^{-}K^{+}\nu$	PRL100(2008)011801	342 fb <sup>-1</sup>	Preliminary ICHEP08	500 fb <sup>-1</sup>
$\tau \rightarrow K^-K^-K^+\nu$	PRL100(2008)011801	342 fb <sup>-1</sup>	Preliminary ICHEP08	500 fb <sup>-1</sup>
			τ−→K <sup>-</sup> φν, PL B643 (2006) 5	
τ <sup>-</sup> →K <sup>-</sup> /K* <sup>-</sup> η ν			Preliminary EPS07 arXiv:0708.0733	485 fb <sup>-1</sup>

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BR( $\tau \rightarrow K^{-} \pi^{0} v_{\tau}$ )

PRD 76:051104, 2007





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Extraction of  $V_{us}$  using  $\tau$  - Data



Extraction of  $V_{us}$  using  $\tau$  - Data



Extraction of  $V_{us}$  using  $\tau$  - Data



$$V_{us}$$
 from  $\tau \rightarrow K \nu$ ,  $\tau \rightarrow \pi \nu$ 



$$\frac{\Gamma(\tau \to K\nu)}{\Gamma(\tau \to \pi\nu)} = \frac{\left|V_{us}\right|^2}{\left|V_{ud}\right|^2} \frac{f_K^2}{f_\pi^2} \left(\frac{1 - m_K^2 / m_\tau^2}{1 - m_\pi^2 / m_\tau^2}\right)^2 \left(1 + \delta_{RC}^{\tau}\right)$$

- Assume universality of couplings
- EW corrections cancel (apart from known long distance corrections  $\delta_{RC}$ )
- Take  $f_K/f_{\pi}$  from Lattice QCD  $f_K/f_{\pi}$ = 1.189±0.007 HPQCD/UKQCD 08
- $|V_{ud}|$  known
- Determine  $B(\tau \rightarrow K \nu)/B(\tau \rightarrow \pi \nu)$







Preliminary  $V_{us}$  from  $\tau \rightarrow Kv$ ,  $\tau \rightarrow \pi v$ 

 $B(\tau \rightarrow K^{-}\nu)/B(\tau \rightarrow \pi^{-}\nu) = 0.06531 \pm 0.00056 \pm 0.00093$ 

$$\frac{\Gamma(\tau \to K\nu)}{\Gamma(\tau \to \pi\nu)} = \frac{|V_{us}|^2}{|V_{ud}|^2} \frac{f_K^2}{f_\pi^2} \left(\frac{1 - m_K^2 / m_\tau^2}{1 - m_\pi^2 / m_\tau^2}\right)^2 \left(1 + \delta_{RC}^\tau\right)$$



 $|V_{us}| = 0.2255 \pm 0.0019 \pm 0.0014$ Perfect agreement with Unitarity

BaBar prel.



Preliminary  $V_{\mu s}$  from  $\tau \rightarrow K \nu$ ,  $\tau \rightarrow \pi \nu$ 

 $\frac{\mathbf{F}(\tau \to K \tau) / \mathbf{B}(\tau \to \pi \tau) = 0.06531 \pm 0.00056 \pm 0.00093}{\Gamma(\tau \to K \tau)} = \frac{|V_{us}|^2}{|V_{ud}|^2} \frac{f_k^2}{f_\pi^2} \left(\frac{1 - m_k^2 / m_\tau^2}{1 - m_\pi^2 / m_\tau^2}\right)^2 \left(1 + \delta_{RC}^{\tau}\right)$ 



|V<sub>us</sub> | = 0.2255±0.0019±0.0014Perfect agreement with Unitarity

**BaBar prel.** 

#### • However:

 $|V_{us}| = 0.2227 \pm 0.0037 \pm 0.0014$  from ratios of PDG08 fit values for  $\tau \rightarrow K\nu$  and  $\tau \rightarrow \pi\nu$  combining these with BaBar value gives:  $0.2249 \pm 0.0017 \pm 0.0014$ 

• With a Belle measurement of same precision as BaBar, can expect error to decrease to  $\pm 0.0013 \pm 0.0014$ 

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## **Conclusions**

Experimental Information on V<sub>us</sub>



Summer 2009 knowledge of  $V_{us}$ 

Experimental Information on  $V_{us}$ 



V<sub>us</sub> determination using τ has potential to get sensitivity of K<sub>13</sub> and K<sub>12</sub> → Completion of the τ strange decay experimental programme → Understand potential issues related to  $\delta R_{\tau}$  (OPE) and  $f_{+}(0)$  for K<sub>13</sub>

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Experimental Information on  $V_{us}$ 



V<sub>us</sub> determination using τ has potential to get sensitivity of K<sub>13</sub> and K<sub>12</sub> → Completion of the τ strange decay experimental programme → Understand potential issues related to  $\delta R_{\tau}$  (OPE) and  $f_{+}(0)$  for K<sub>13</sub>

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## $|V_{us}|$ using different weight functions in

*FESR to provide*  $\delta R_{OPE}^{w}$ 



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### *Combination of tau and e+e- data in FESR*



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## Comments on 3 Sigma Tension in FESR $\tau$

- Still need to complete the programme of measurements – so ~3σ discrepancy in FESR |V<sub>us</sub>| most probably will go away
- If  $3\sigma$  discrepancy in FESR  $|V_{us}|$  increases in significance, may need to consider theories/models that accommodate a tau FESR  $|V_{us}|$  different from the pseudo-scalar ratio determination of  $|V_{us}|$
- Perhaps a 3<sup>rd</sup> generation lepton coupling that cancels in the pseudoscalar ratio(?)
- Perhaps something that is more sensitive to final state hadronic system with spin=1(?)
- Lepto-quarks come to mind (?)

#### Callan - Treiman Relation

$$\begin{split} t_{\rm CT} &= {m_K}^2 - {m_\pi}^2 \\ \Delta_{\rm CT} &= SU(2) \text{-breaking correction} \\ &= -(3.5 \pm 8.0) \times 10^{-3} \\ &\quad \text{in NLO ChPT } (m_u = m_d) \end{split}$$

KLOE

**ISTRA+** 

**NA48** 

**KTeV** 

0.9

0.95

#### in NLO ChPT $(m_u = m_d)$ UKQCD/RBC UKQCD/RBC USe C Net Kaon WG $\lambda_0^{C}$ $\lambda_0^{C}$

1

 $f_{+}(0)$ 

1.05

#### Callan-Treiman relation:

$$\tilde{f}_0(t_{\rm CT}) = \frac{f_K}{f_\pi} \frac{1}{f_+(0)} + \Delta_{CT}$$

Use dispersive parameterization of  $f_0(t)$ 

KLOE  $K_{e3-\mu3}$  data:  $\lambda_0^{\ C} = (14.0 \pm 2.1) \times 10^{-3}$  $\rightarrow f_+(0) = 0.968(28)$ 

NA48  $K_{\mu 3}$  data: In C = 0.1438(138)  $\rightarrow f_{+}(0) = 1.027(20)$ 

Lattice QCD  $f_{+}(0) = 0.964(5)$ 

**Extracting**  $|V_{us}|$ The weighted spectral functions  $R_{\tau,ij}^{w}(s_0) = \int_{0}^{s_0} ds \ w(s) \frac{dR_{\tau,ij}}{ds}$  (*ij* = *ud* or *us*) may be written as:  $P_{\tau,ij}^{w}(s_0) = \sum_{0}^{s_0} (|V_{\tau}|^2 s^{kl}(P_{\tau}) + |V_{\tau}|^2 s^{kl}(P_{\tau}))$ 

$$R_{\tau,ij}^{w}(s_{0}) = 3S_{EW} \left\{ \left( \left| V_{ud} \right|^{2} + \left| V_{us} \right|^{2} \right) \left( 1 + \delta^{kl(0)} \right) + \sum_{D \ge 2} \left( \left| V_{ud} \right|^{2} \delta_{ud}^{kl(D)} + \left| V_{us} \right|^{2} \delta_{us}^{kl(D)} \right) \right\}$$

When one takes the flavour breaking difference,

$$\delta R_{\tau}^{w}(s_{0}) = \frac{R_{\tau,ud}^{w}(s_{0})}{|V_{ud}|^{2}} - \frac{R_{\tau,us}^{w}(s_{0})}{|V_{us}|^{2}}$$

the D=0 terms cancel leaving D $\geq$  2. Thus:

$$|V_{us}| = \sqrt{\frac{R_{us}^{w}(s_{0})}{(R_{ud}^{w}(s_{0})/|V_{ud}|^{2}) - \delta R_{OPE}^{w}(s_{0})}}$$

where  $\delta R_{OPE}^{w}(s_0)$  must be calculated and  $R_{ij}^{w}(s_0)$  measured Note: Because the D=0 term is significantly greater than the D=2 term, a large uncertainty on the OPE expansion still yields a small uncertainty on  $|V_{us}|$ 

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# Extracting $|V_{us}|$ from $\tau$ -Spectral Function Strange and non-strange Hadronic Width $R_{\tau,ij} = \frac{Br(\tau^- \rightarrow v_{\tau}hadrons_{ij}^-)}{Br(\tau^- \rightarrow v_{\tau}\overline{v_e}e^-)}$ where ij = ud or us

May be written in terms of the spectral density function

$$R_{ij} = 12S_{EW}\pi^2 |V_{ij}|^2 \int_{0}^{m_{\tau}^2} \left(1 - \frac{s}{m_{\tau}^2}\right)^2 \left[\left(1 + \frac{2s}{m_{\tau}^2}\right)\rho_{ij}^{(1)}(s) + \rho_{ij}^{(0)}(s)\right] \frac{ds}{m_{\tau}^2}$$

or in terms of the 2 point correlator function

$$R_{ij} = 12S_{EW}\pi \left|V_{ij}\right|^2 \frac{-1}{2\pi i} \oint_{|s|=m_r^2} \left(1 - \frac{s}{m_r^2}\right)^2 \left[\left(1 + \frac{2s}{m_r^2}\right)\Pi_{ij}^{(1)}(s) + \Pi_{ij}^{(0)}(s)\right] \frac{ds}{m_r^2}$$

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e.g. A set of 'spectral moments' has been used in the FESR as the particular weight functions w

$$R_{\tau,ij}^{kl} = \int_{0}^{s_0} ds \left(1 - \frac{s}{m_{\tau}^2}\right)^k \left(\frac{s}{m_{\tau}^2}\right)^l \left(\frac{dR_{\tau,ij}}{ds}\right)$$

For (k,l)=(0,0), R<sup>00</sup> is obtained from the BR of strange decays

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$$V_{ud} from 0+ \rightarrow 0+$$

$$V_{ud} from 0+$$

#### Lepton Universality from prel. BaBar result





For phase space integral need to parameterize and measure FF-dependence on t



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The 2004 Kaon Revolution:  $K_{l3}$  BR's

