

# Di-photon coupling of $f_0(600)$ , $f_0(980)$ , $f_2(1270)$ resonances and $g_{\sigma\pi\pi}^2$

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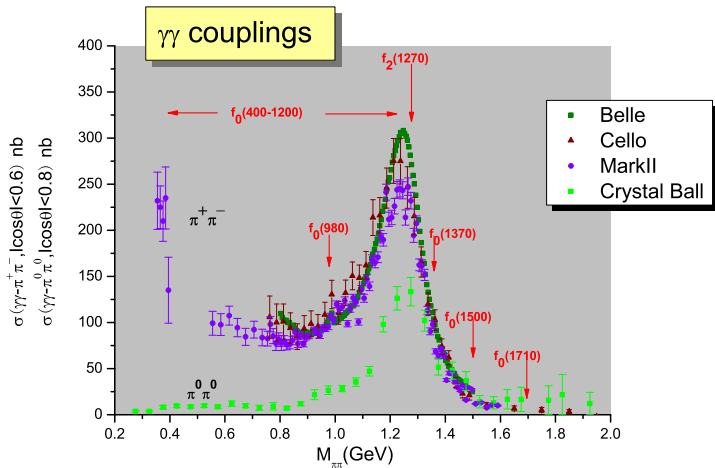
Chiral Dynamics 2009, July 6 - 10, 2009, Bern

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<sup>1</sup>Representing L. C. Jin, Y. Mao, X. G. Wang, Ou Zhang, Z. Y. Zhou

# Table of contents

- ▶  $\gamma\gamma \rightarrow \pi\pi$  data and di-photon coupling of resonances
- ▶ The  $\sigma\pi\pi$  coupling and the information it provides.

$\gamma\gamma \rightarrow \pi\pi$  dataT. Mori *et al.* (Belle Collaboration) 07;

M. R. Pennington, *Mod. Phys. Lett. A*22(2007)1439.

composition	prediction	author(s)
$(\bar{u}u + \bar{d}d)/\sqrt{2}$	4.0	Babcock and Rosner 76
$\bar{s}s$	0.2	Barnes 85
$gg$	0.2 ~ 0.6	Narison 06
$[ns][\bar{n}s]$	0.27	Achasov <i>et al</i> 82
$\bar{K}K$	0.6	Barnes 92
	0.22	Hanhart 07

**Table:** Summary of two photon decay width of scalars calculated in different models.

- D. Morgan, M. R. Pennington, Z. Phys. **C48**(1990)623.  
G. Mennessier, Z. Phys. **C16**(1983)241.  
A. V. Anisovich, V. V. Anisovich, Phys. Lett. **B467**(1999)289.  
L. V. Fil'kov, V. L. Kashevarov, Phys. Rev. **C72**(2005)035211.  
N. N. Achasov, G. N. Shestakov, arXive:0712.0885 [hep-ph].  
J. A. Oller, L. Roca, C. Schat, Phys. Lett. **B659**(2008)201.  
J. Bernabeu, J. Prades, Phys. Rev. Lett. **100**(2008)241804.  
G. Mennessier, S. Narison, W. Ochs, Phys. Lett. **B665**(2008)205.  
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## A couple channel calculation in $IJ=00$ channel

Y. Mao et al., arXiv:0904.1445 v2, to appear in PRD  
(Babelon et al. 76; Donoghue, Holstein 93; Morgan, Pennington 91):

$$F(s) = F_B + D(s) \left[ P s - \frac{s^2}{\pi} \int_{4m_\pi^2}^{\infty} \frac{\text{Im} D^{-1}(s') F_B(s')}{s'^2 (s' - s - i\epsilon)} ds' \right]. \quad (1)$$

2 by 2 matrix  $D$  only contains *r.h.c.* and satisfies couple channel unitarity; iteration method.

$$\begin{aligned} \text{Im} D_{11} &= D_{11} \rho_1 T_{11}^* \theta_1 + D_{21} \rho_2 T_{12}^* \theta_2, \\ \text{Im} D_{21} &= D_{11} \rho_1 T_{21}^* \theta_1 + D_{21} \rho_2 T_{22}^* \theta_2; \end{aligned} \quad (2)$$

$F_B$  Born term amplitudes:  $\pi + V + A +$  exponential form-factor.  
Single channel approx. for other channels  $\Rightarrow D = \text{Omnés function}$ .

## Couple channel $T$ matrix

$K_3$  fit of Au, Morgan, Pennington 88;  
Refit by adding Pislak et al. 03:

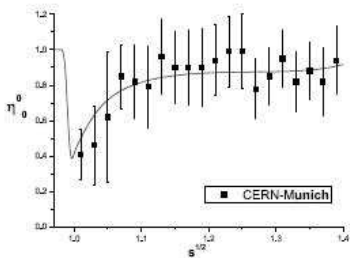
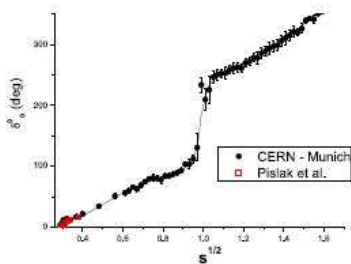


Figure 2: The fit curve of  $\pi\pi$   $I = 0$  S-wave phase shift and inelasticity with CERN-Munich data [20] and data from Pislak et al. [21].

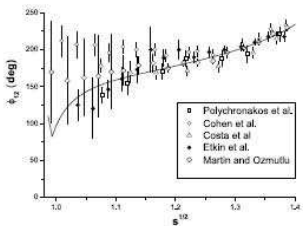


Figure 3: The phase shift  $\phi_{12} = \delta_\pi + \delta_K$  of  $\pi\pi \rightarrow K\bar{K}$   $I = 0$  S-wave scattering with data sets from Res. [22, 23, 24, 25, 26]. Notice that Ref. [22] is not used in the fit.



## Poles from $K_3$ matrix fit

pole	sheet-II	sheet-III
$\sigma$	0.507 - 0.229i	0.638 - 0.165 i
$f_0(980)$	0.994 - 0.019 i	0.984 - 0.033 i

Table: The poles's location on the  $\sqrt{s}$ -plane, in units of GeV.

Breit-Wigner description of  $f_0(980)$ ?

“Ambiversion of X(3872)”, [Ou Zhang et al., arXiv:0901.1553](#)

	Pole-positions(GeV)	$\Gamma(f_J \rightarrow \gamma\gamma)$ (keV)
$f_0^{II}(980)$	$0.999 - 0.021i$	0.12
$f_0^{III}(980)$	$0.977 - 0.060i$	0.35
$f_0(600)$	$0.549 - 0.230i$	0.76
$f_2(1270)(\lambda = 0)$	$1.272 - 0.087i$	0.66
$f_2(1270)(\lambda = 2)$		3.70

Table: Di-photon decay width of poles

$\lambda = 2$  dominates;  $\Gamma_{f_2(1270) \rightarrow 2\gamma}(4.36 \text{keV}) >$

$\Gamma(\text{Pennington08})(3.82 \pm 0.30) > \Gamma(\text{PDG})(3.03 \pm 0.35)$  ;  $f_0^{II}(980)$

width agrees with [M. R. Pennington, T. Mori, S. Uehara, Y.](#)

[Watanabe, Eur. Phys. J.C56\(2008\)1](#);  $\Gamma(f_0(600) \rightarrow 2\gamma)$  very small.

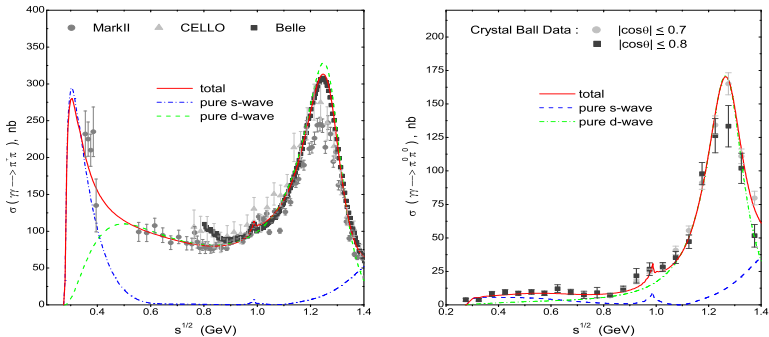
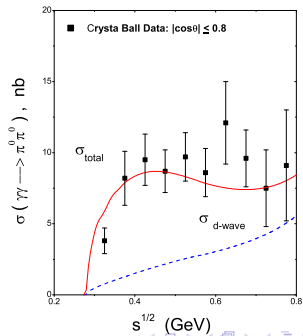
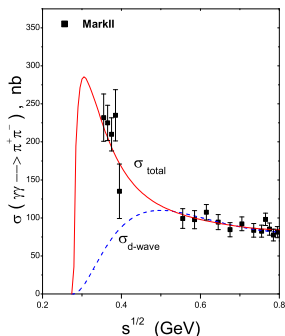


Figure: The coupled channel fit to the  $\gamma\gamma \rightarrow \pi^+\pi^-$ ,  $\pi^0\pi^0$  data.

## A refined fit using single channel amplitude

T matrix from [Zhou et al. 05](#)

upto 800MeV; one parameter fit; others fixed by couple channel fit and treated as background.



$\chi^2$	pole location	$\Gamma(\sigma \rightarrow \gamma\gamma)$ (keV)
0.8	$0.456 - 0.276i$	2.08

Table: One parameter fit up to 0.8GeV of data.

- ▶ Non  $\bar{q}q$  meson.
- ▶ Chiral partner of Nambu-Goldstone bosons in a linearly realized chiral symmetry.

## $g_{\sigma\pi\pi}^2$ couplings

T matrix from Zhou et al., JHEP 0502(2005)043  $\Rightarrow$

$$M_\sigma = 457\text{MeV} , \quad \Gamma_\sigma = 551\text{MeV} ,$$

and the residue:

$$g_{\sigma\pi\pi}^2 = (-0.20 - 0.13i)\text{GeV}^2 .$$

G. Mennessier, S. Narison, W. Ochs, Phys. Lett. B665(2008)205:

$$g_{\sigma\pi\pi}^2 = (-0.25 - 0.06i)\text{GeV}^2 .$$

$\text{Re}[g^2] < 0!$

# The PKU representation

$$S^{phy.} = S^{f_0(600)} \times \prod_i S^{R_i} \cdot S^{cut} .$$

$$S^R(s) = \frac{M^2(z_0) - s + i\rho(s)sG[z_0]}{M^2(z_0) - s - i\rho(s)sG[z_0]} ,$$

$$M^2(z_0) = \text{Re}[z_0] + \frac{\text{Im}[z_0] \text{Im}[z_0 \rho(z_0)]}{\text{Re}[z_0 \rho(z_0)]} , \quad G[z_0] = \frac{\text{Im}[z_0]}{\text{Re}[z_0 \rho(z_0)]} .$$

Mainly a kinematical effect?: Neglecting everything rather than  $f_0(600)$ ,

$$g_{\sigma\pi\pi}^2 = (-0.18 - 0.20i)\text{GeV}^2 .$$

More than a pure kinematical effect!

# The $O(N)$ model, v1

$$T^{00}(s) = \frac{1}{32\pi} \frac{s - m_\pi^2}{f_\pi^2 - (s - m_\pi^2) \left( \frac{1}{\lambda_0} + \tilde{B}_0(s) \right)}$$

$$\tilde{B}_0(p^2) = \frac{-i}{2} \int \frac{d^4q}{(2\pi)^4} \frac{1}{q^2 - m_\pi^2} \frac{1}{(p+q)^2 - m_\pi^2}$$

Renormalization:

$$\frac{1}{\lambda(M)} = \frac{1}{\lambda_0} - \frac{i}{2} \int \frac{d^4q}{(2\pi)^4} \frac{1}{(q^2 + i\epsilon)(q^2 - M^2 + i\epsilon)}, \quad (3)$$

$$\frac{1}{\lambda(M)} + \tilde{B}(p^2; M) = \frac{1}{\lambda_0} + \tilde{B}_0(p^2).$$

$$\tilde{B}(s; M) = \frac{1}{32\pi^2} \left[ 1 + \rho(s) \log \frac{\rho(s) - 1}{\rho(s) + 1} - \log \frac{m_\pi^2}{M^2} \right]$$



## Chivukula, Golden 92

$$\mu^2 \frac{d\lambda}{d\mu^2} = \frac{\lambda^2(\mu^2)}{32\pi^2} . \quad (4)$$

To define the theory:

$$\frac{1}{\lambda(M)} = 0 .$$

$M$  denotes the scale where perturbation expansion fails –

The theory is still fine!

However, **Tachyon occurs** at  $m_t^2$ . Theory only works when  $|s| \ll |m_t^2|$ .

## The $O(N)$ model, v2

Sharp momentum cutoff at  $\Lambda$ :

No tachyon. Spurious cut and spurious pole nearby, instead.  
Cutoff version of effective theory.

Set for example

$$\frac{1}{\lambda(\Lambda)} = 0 ,$$

defines (another) theory.

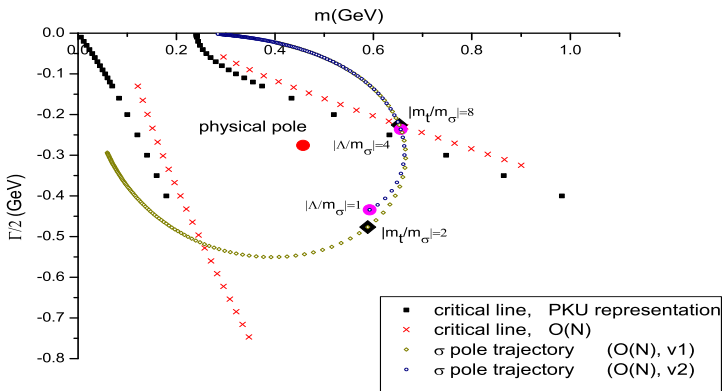


Figure: Region on the  $\sqrt{s}$ -plane with  $\text{Re}[g_{\sigma\pi\pi}^2] < 0$ .

Furthermore, to get the 'real' sigma pole position,  $\lambda(M)$  blows up at very low value:

$$\lambda(M \sim .55\text{GeV}) = \infty .$$

Conclusion: The “ $\sigma$ ” pole manifests the extreme ‘nonperturbativity’ that QCD could offer.

Thanks for patience!